

Dynamical Mean-Field Theory on the Real-Frequency Axis: p-d Hybridizations and Atomic Physics in SrMnO₃

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We investigate the electronic structure of SrMnO₃ with Density Functional Theory (DFT) plus Dynamical Mean-Field Theory (DMFT). Within this scheme the selection of the correlated subspace and the construction of the corresponding Wannier functions is a crucial step. Due to the crystal field splitting of the Mn-3*d* orbitals and their separation from the O-2*p* bands, SrMnO₃ is a material where on first sight a 3-band *d*-only model should be sufficient. However, in the present work we demonstrate that the resulting spectrum is considerably influenced by the number of correlated orbitals and the number of bands included in the Wannier function construction. For example, in a *d-dp* model we observe a splitting of the *t*_{2*g*} lower Hubbard band into a more complex spectral structure, not observable in *d*-only models. To illustrate these high-frequency differences we employ the recently developed Fork Tensor Product State (FTPS) impurity solver, as it provides the necessary spectral resolution on the real-frequency axis. We find that the spectral structure of a 5-band *d-dp* model is in good agreement with PES and XAS experiments. Our results demonstrate that the FTPS solver is capable of performing full 5-band DMFT calculations directly on the real-frequency axis.

I. INTRODUCTION

The combination of density functional theory (DFT) and dynamical mean-field theory (DMFT) has become the work-horse method for the modeling of strongly-correlated materials¹⁻³. For DMFT, a (multi-orbital) Hubbard model is constructed in a selected correlated subspace, which usually describes the valence electrons of the transition metal orbitals in a material. An adequate basis for these localized orbitals are projective Wannier functions^{4,5}. In contrast to the Bloch wave functions, these functions are localized in real space, and therefore provide a natural basis to include local interactions as they resemble atomic orbitals and decay with increasing distance from the nuclei. However, the selection of the correlated subspace itself and the Wannier function construction are not uniquely defined.

In the present work, we use SrMnO₃ to analyze the differences of some common models. This perovskite is an insulator⁶ with a nominal filling of three electrons in the Mn 3*d* shell. There are various works concerning its electronic structure, both on the experimental⁷⁻¹² as well as on the theoretical side¹³⁻¹⁶. For the construction of the correlated subspace, we explicitly identify the following meaningful cases: The first is a three orbital model for the *t*_{2*g*} states only. For the second choice, usually denoted as *d-dp* model, the transition metal 3*d*-states and the oxygen 2*p*-states are considered in the Wannier function construction, but the Hubbard interaction is only applied to the 3*d*-states. The correlated subspace is then affected by the lower lying oxygen bands due to hybridizations. In both cases, the full 3*d* manifold can be retained by including the *e*_g orbitals in genuine 5 orbital models. To assess the consequences of the different low-energy

models, a good resolution of the spectral function on the real-frequency axis is beneficial. Due to its exactness up to statistical noise, Continuous Time Quantum Monte Carlo (CTQMC) is often used as a DMFT impurity solver¹⁷⁻¹⁹. However, when using a CTQMC impurity solver, an analytic continuation is necessary, which results in spectral functions with a severely limited resolution at higher frequencies²⁰. This can make it difficult to judge the influence of the choices made for the correlated subspace. In the present paper, we therefore employ the real-frequency Fork Tensor Product States (FTPS) solver²⁰. This recently developed zero temperature impurity solver was previously applied to SrVO₃, making it possible to reveal an atomic multiplet structure in the upper Hubbard band²⁰. This observation of a distinct multiplet structure in a real-material calculation is an important affirmation of the atom-centered view promoted by DMFT.

The present work also serves as a deeper investigation of the capabilities of the FTPS solver. We show that the FTPS solver can be applied to *d-dp* models, leading to new insight into the interplay of the atomic physics of the transition metal impurity and hybridization effects with the oxygen atoms as a natural extension to the atom-centered view. Furthermore, the physics of SrMnO₃ is different from SrVO₃, since the manganate is an insulator, and thus it constitutes a new challenge for the FTPS solver. While we presented a proof of concept for FTPS on a simple 5-band model before²⁰, we now perform full 5-band real-frequency DFT+DMFT calculations for both *d*-only and *d-dp* models.

We find that the choices made for the correlated subspace strongly affect the resulting spectral function and its physical interpretation. Additionally, we show that

the interplay of atomic and hybridization physics can already be found in very simple toy models.

This paper is structured as follows. In section II we discuss the methods employed, namely DFT, the different models obtained from different Wannier constructions, DMFT, and the impurity solvers used. Section III focuses on the results of the DMFT calculations and the underlying physics of these different models. This knowledge will then be used in Sec. IV to compare the spectral function to experiments by Kim *et al.*¹².

II. METHOD

A. DFT and WANNIER BASIS

We start with the DFT density of states (DOS) from a non-spin-polarized DFT calculation for SrMnO₃ in the cubic phase (shown in Fig. 1). The calculation was performed with Wien2k²¹, using 969 k -points in the irreducible Brillouin zone and a lattice parameter of $a = 3.768 \text{ \AA}$. Around the Fermi energy E_F , SrMnO₃ has the characteristic steeple-like shaped DOS, stemming from the Mn- t_{2g} bands with a bit of O- $p_{x/y}$ contribution. Below -2.0 eV , the DOS is mainly determined by oxygen bands which also exhibit manganese hybridizations. With the exception of some additional weight below -5.0 eV , the Mn- e_g states lie mainly in the energy range from 0.0 eV to 5.0 eV .

In this work we use projective Wannier functions, where an energy interval has to be chosen as a projection window^{4,5}. The bands around E_F have mainly t_{2g} character, suggesting a selection of only a narrow energy window for the Wannier function construction (-2.0 eV to 0.82 eV). We call this set of projective Wannier functions the 3-band d -only model. However, the t_{2g} orbitals also show a considerable hybridization with the O- $2p$ states below -2 eV , and hence, one might want to enlarge the projective energy window by setting its lower boundary to -10 eV . We refer to this model as the 3-band d - dp model.

At the same time, we realize that also the e_g orbitals are not entirely separated from the t_{2g} orbitals in energy and that they have even some weight around E_F (see middle graph of Fig. 1). These states lie directly above E_F and therefore their influence on the resulting spectrum needs to be checked. One should then use a window capturing 5 bands, the e_g and t_{2g} , as a correlated subspace (from -2 eV to 5 eV). This is a 5-band d -only model. Note that empty orbitals do not pose a problem for the FTSP solver. Like before, we can again enlarge the energy window to include the oxygen hybridization (-10 eV to 5 eV). We denote this model as the 5-band d - dp model.

In total, we end up with 4 different choices. The settings for these 4 models are summarized in Tab. I. All of them are justified, have different descriptive power, and have been employed in various DFT+DMFT calculations for

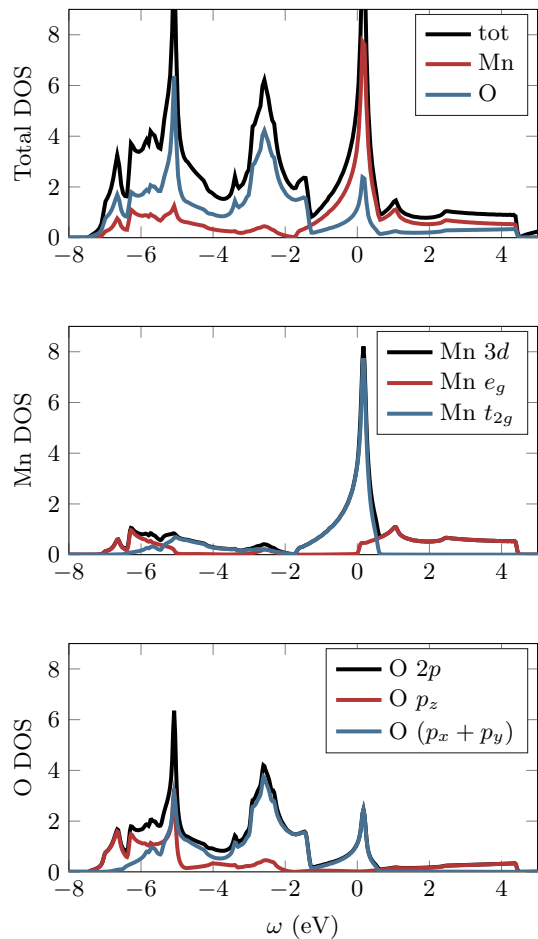


FIG. 1. *Top*: Total DFT-DOS for SrMnO₃. *Middle*: partial Mn- $3d$ DOS. *Bottom*: partial O- $2p$ DOS for SrMnO₃. Below approximately -1.5 eV , the band structure consists of oxygen bands that have mostly p -character but also have some e_g and t_{2g} weight due to hybridizations. The t_{2g} bands are located around the Fermi energy from -1.5 eV to about 0.5 eV , which have small p -character. Directly above the Fermi energy and partly overlapping with the t_{2g} bands we find the e_g bands that have small p -contributions as well.

SrMnO₃^{13,14,16}.

B. DMFT

Once the correlated subspace is defined, we use DMFT^{2,3,22,23} to solve the resulting multi-band Hubbard model. As interaction term we choose the 5/3-band Kanamori Hamiltonian²⁴. Within DMFT, the lattice problem is mapped self consistently onto an Anderson impurity model (AIM) with the Hamiltonian

TABLE I. Summary of models with their projective energy windows and the parameters used in the FTFS solver: number of bath sites N_B , Fourier transform broadening η_{FT} , truncated weight t_w and maximal bond dimension allowed for the links between impurities as well as for the links between an impurity and the first bath tensor. We keep at most this number of states and increase t_w if needed. The number in brackets is the maximal bond dimension during ground state search, while the first number is used for the time evolution. The bath links were not restricted to any maximal bond dimension. The FTFS time evolution is performed up to t_{max} , given in eV^{-1} .

| Model | Window (eV) | Comments | N_B | η_{FT} | t_w | Bond dim. | t_{max} |
|--------------------------|-------------|--|-------|-------------|-------------------|-----------|-----------|
| 3-band d -only | -2.0 - 0.82 | only major t_{2g} weight around E_F | 79 | 0.08 | $5 \cdot 10^{-9}$ | - | 14.0 |
| 5-band d -only | -2.0 - 5.0 | include e_g , neglect hybridizations | 49 | 0.15 | $1 \cdot 10^{-8}$ | 200 (150) | 12.0 |
| 3-band d - dp -model | -10.0 - 5.0 | include hybridized t_{2g} weight on oxygen bands | 59 | 0.1 | $1 \cdot 10^{-8}$ | 450 (150) | 14.0 |
| 5-band d - dp -model | -10.0 - 5.0 | t_{2g} and e_g bands with hybridizations | 49 | 0.2 | $1 \cdot 10^{-8}$ | 200 (150) | 7.0 |

$$\begin{aligned}
H &= H_{\text{loc}} + H_{\text{bath}} \\
H_{\text{loc}} &= \sum_{m\sigma} \epsilon_{m0} n_{m0\sigma} + H_{\text{DD}} + H_{\text{SF-PH}} \\
H_{\text{DD}} &= U \sum_m n_{m0\uparrow} n_{m0\downarrow} \\
&\quad + (U - 2J) \sum_{m' > m, \sigma} n_{m0\sigma} n_{m'0\bar{\sigma}} \\
&\quad + (U - 3J) \sum_{m' > m, \sigma} n_{m0\sigma} n_{m'0\sigma} \\
H_{\text{SF-PH}} &= J \sum_{m' > m} \left(c_{m0\uparrow}^\dagger c_{m0\downarrow} c_{m'0\uparrow} c_{m'0\downarrow}^\dagger + \text{h.c.} \right) \\
&\quad - J \sum_{m' > m} \left(c_{m0\uparrow}^\dagger c_{m0\downarrow}^\dagger c_{m'0\uparrow} c_{m'0\downarrow} + \text{h.c.} \right) \\
H_{\text{bath}} &= \sum_{ml\sigma} \epsilon_{ml} n_{ml\sigma} + V_{ml} \left(c_{m0\sigma}^\dagger c_{ml\sigma} + \text{h.c.} \right).
\end{aligned} \tag{1}$$

Here, $c_{ml\sigma}^\dagger$ ($c_{ml\sigma}$) creates (annihilates) an electron in orbital m , with spin σ at site l (site zero is the impurity). $n_{ml\sigma}$ are the corresponding particle number operators. ϵ_{m0} is the orbital dependent on-site energy of the impurity and ϵ_{ml} as well as V_{ml} are the bath on-site energies and the bath-impurity hybridizations, respectively. The interaction part of Hamiltonian (1), $H_{\text{DD}} + H_{\text{SF-PH}}$, is parametrized by a repulsive interaction U and the Hund's coupling J . For each of the models presented in Tab. I, we choose these parameters *ad hoc* in order to obtain qualitatively reasonable results. In addition, for the full 5-band d - dp model we also estimate them quantitatively via a comparison to an experiment. Within DFT+DMFT, a so-called double counting (DC) correction is necessary, because part of the electronic correlations are already accounted for by DFT. For general cases, exact expressions for the DC are not known, although there exist several approximations²⁵⁻²⁸. In the present work we use the fully-localized-limit (FLL) DC (Eq.(45) in Ref. 29). When needed, we adjust it to account for deviations from the true, unknown DC. Note

that in the d -only models, the DC is a trivial energy shift that can be absorbed into the chemical potential²⁷, which is already adjusted to obtain the correct number of electrons in the Brillouin zone. This step, as well as all other interfacing between DFT and DMFT, is performed using the TRIQS/DFTTools package (v1.4)^{5,30-32}.

C. CTQMC + MaxEnt

We compare some of our results to CTQMC data at an inverse temperature of $\beta = 100 eV^{-1}$ obtained with the TRIQS/CTHYB solver (v1.4)^{17,33}. We calculate real-frequency spectra with an analytic continuation using the freely available Ω -MaxEnt implementation of the Maximum Entropy (MaxEnt) method³⁴. However, the analytic continuation fails to reproduce high-energy structure in the spectral function, as we have shown in Ref.²⁰ on the example of SrVO₃. This is especially true when the imaginary-time Green's function is subject to statistical noise, which is inherent to Monte Carlo methods.

D. FTFS

For all models studied we employ FTFS²⁰. This recently developed impurity solver uses a tensor network geometry which is especially suited for AIMs. The first step of this temperature $T = 0$ method is to find the absolute ground state including all particle number sectors with DMRG³⁵. Then the interacting impurity Green's function is calculated by real-time evolution. Since entanglement growth during time evolution prohibits access to arbitrary long times³⁶, we calculate the Green's function up to some finite time (see Tab. I) and predict the time series using the linear prediction method^{20,37} up to times $\mathcal{O}(100 eV^{-1})$. The linear prediction could potentially produce artifacts in the spectrum, and therefore we always make sure that every spectral feature discussed in this work is already present in the finite-time Green's function without linear prediction.

The main approximations that influence the result of the FTPS solver are the broadening η_{FT} used in the Fourier transform³⁸, and the truncation of the tensor network²⁰. The former corresponds to a convolution with a Lorentzian in frequency space making its influence predictable, while the truncation can be controlled by including more states. This control over the approximations allows us to analyze spectral functions in greater detail than what would be possible with CTQMC+MaxEnt. The parameter values for our FTPS calculations are listed in Tab. I.

Note that we choose η_{FT} larger than in our previous work²⁰. The reason for doing this is two-fold: First, some of the calculations we show in this work have a large bandwidth, which lowers the energy resolution if we keep the number of bath sites fixed. Second, FTPS uses a discretized bath to represent the continuous non-interacting lattice Green's function G_0^{cont} . When calculating the self energy $\Sigma = G_0^{-1} - G^{-1}$, we can either use the discretized version of G_0^{discr} or the continuous one, G_0^{cont} . In this work we choose G_0^{discr} , which is formally the correct choice. This then requires to use a larger broadening to obtain causal self energies that do not show finite discretization effects from inverting G_0^{discr} . However, when calculating the final impurity spectral function shown in all figures, we employ a very small broadening of $\eta_{FT} = 0.01$ eV in order to obtain optimal resolution.

The real-frequency approach of FTPS allows to resolve spectral features with higher precision than CTQMC+MaxEnt. This is especially true for high energy multiplets. On the other hand, with FTPS and real-time evolution it is difficult to obtain perfect gaps, since the results are less precise at small ω , encoded in the long-time properties of the Green's function which we obtain only approximately using linear prediction³⁷. With FTPS we calculate the greater and lesser Green's functions separately²⁰. Since the greater (lesser) Green's function has no contribution at $\omega < 0$ ($\omega > 0$) we restricted the contributions of the calculated Green's functions in frequency space.

III. RESULTS

A. *d*-only models

First we focus on *d*-only calculations using a projective energy window with a lower energy boundary of -2.0 eV for the Wannier-function construction, neglecting the occupied Mn-3*d* weight at lower energies (see Tab. I and middle graph of Fig. 1). With this choice of the correlated subspace, the occupation of the e_g orbitals is nearly zero and the three degenerate t_{2g} orbitals are half-filled.

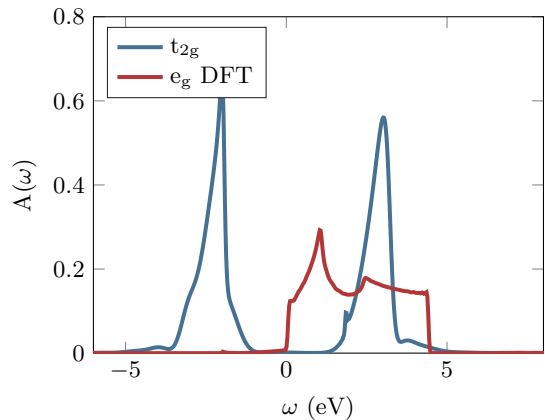


FIG. 2. 3-band *d*-only calculation: t_{2g} correlated spectral function for $U = 4.0$ eV and $J = 0.6$ eV, as well as e_g DFT-DOS. The t_{2g} spectrum shows a Mott insulator at half-filling with pronounced lower and upper Hubbard bands.

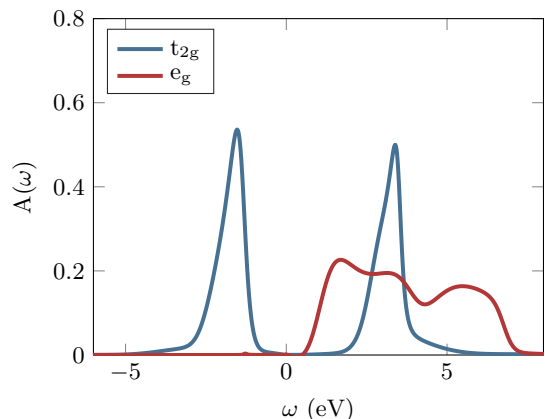


FIG. 3. 5-band *d*-only calculation: correlated spectral function of the e_g and the t_{2g} orbitals for $U = 4.0$ eV and $J = 0.6$ eV.

3-band calculation

Considering only the t_{2g} subspace, the resulting impurity spectral function (Fig. 2) is gapped for the chosen interaction values. The peaks of the lower and upper Hubbard bands are separated by 5.0 eV in energy, which is roughly $U + 2J = 5.2$ eV, as expected from atomic physics³⁹.

Contrary to SrVO₃, where a distinct 3-peak multiplet structure in the upper Hubbard band is present²⁰, both SrMnO₃ Hubbard bands show only one dominant peak. The structure observed in SrVO₃ was well explained by the atomic multiplets of the interaction Hamiltonian H_{loc} in Eq. 1 for a ground state with one electron occupying the t_{2g} orbitals. The absence of such an atomic multiplet structure in this model for SrMnO₃ can be understood in a similar way: The large Coulomb repulsion in combination with Hund's rules (due to the density-density

interaction strengths U , $U - 2J$ and $U - 3J$) lead to a ground state $|\psi_0\rangle$ which consists mostly of the states $|\uparrow, \uparrow, \uparrow\rangle$ and $|\downarrow, \downarrow, \downarrow\rangle$ on the impurity. Adding a particle, when calculating the Green's function, produces a single double occupation, e.g., $c_{1,\downarrow}^\dagger |\psi_0\rangle = |\uparrow\downarrow, \uparrow, \uparrow\rangle$. This state is an eigenstate of the atomic Hamiltonian, because it is trivially an eigenstate of H_{DD} , and both the spin-flip and pair-hopping terms annihilate this state. Hence, all t_{2g} single-particle excitations from the ground state have the same energy, and as a consequence, only *one* atomic excitation energy is observed.

Although not included in the low-energy model, the uncorrelated states still need to be taken into account for the single-particle gap of SrMnO₃. On the unoccupied side, the onset of the e_g orbitals leads to a reduction of the single-particle gap to about half the size of the t_{2g} gap (see Fig. 2). On the occupied side, depending on U and J , either the lower Hubbard band or the O-bands (at about -1.5 eV) determine the gap size, and thus also the type of the insulating state (Mott or charge transfer insulator⁴⁰). For SrMnO₃ to be clearly classified as Mott insulator, $U + 2J < 3.0$ eV would be required. However, it is questionable if the d -only picture is correct, as in this case the lower Hubbard band is not influenced by the $t_{2g}/O-2p$ hybridizations between -6.0 eV and -2.0 eV (see Fig 1). We will discuss the effect of these hybridizations in detail in Sec. III B and Sec. III C.

5-band calculation

Next, we add the e_g orbitals to the correlated subspace, which now comprises the full Mn-3d manifold. The resulting impurity spectral functions of the e_g and t_{2g} orbitals are shown in Fig. 3. The t_{2g} spectral weight does not change much compared to the 3-band calculation. This is to be expected, because the e_g orbitals remain nearly empty during the calculation of the t_{2g} Green's function.

The e_g spectral function, on the other hand, becomes much broader in comparison to the DFT-DOS, showing spectral weight above 4.5 eV. The unoccupied part of the spectrum is encoded in the greater Green's function, i.e., adding a particle in an e_g orbital to the ground state. If we again assume $|\psi_0\rangle \propto |\uparrow, \uparrow, \uparrow\rangle + |\downarrow, \downarrow, \downarrow\rangle$ as the t_{2g} ground state, we can add a particle to the e_g orbitals either in a high-spin or low-spin configuration:

$$c_{e_g, \uparrow}^\dagger |\psi_0\rangle \propto \underbrace{|\uparrow, \uparrow, \uparrow\rangle}_{t_{2g}} \otimes \underbrace{|\uparrow, 0\rangle}_{e_g} + |\downarrow, \downarrow, \downarrow\rangle \otimes |\uparrow, 0\rangle. \quad (2)$$

Using the Kanamori Hamiltonian, the high-spin configuration (first term in Eq. 2) generates a single atomic excitation energy, while the low-spin configuration (second term in Eq. 2) leads to two energies (due to the spin-flip terms). According to this atomistic picture, the splitting of the e_g peaks is proportional to Hund's coupling J (see Fig. 3). Their position relative to the upper t_{2g} Hubbard band is influenced by the crystal field splitting and

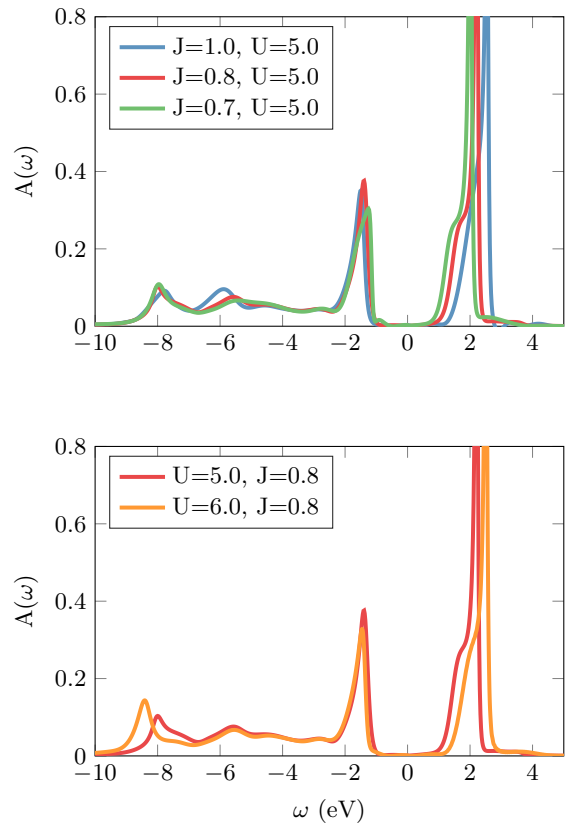


FIG. 4. 3-band d - dp model: spectral functions for different J (top) and different U (bottom). All interaction parameters are given in eV. Upon increasing both parameters the gap increases. Changing J shifts the peak at around -6.0 eV, while changing U only shifts the one at -8.0 eV.

J . From this clear atomic-like structure we see that even empty orbitals need to be included in the correlated subspace because of correlation effects with other occupied orbitals.

B. 3-band d - dp model

In the energy region where the lower Hubbard band is located, we also find t_{2g} weight stemming from the Mn-3d/ $O-2p$ hybridization (see middle plot of Fig. 1). This suggests that those states should be included in the construction of the projective Wannier functions, i.e., a d - dp model. In the following we will use the term High Energy Spectral Weight (HESW) to denote the Wannier function weight on the oxygen bands (located below -1.5 eV). The first and most obvious consequence of a larger projective energy window is an increased bandwidth of the Wannier DOS. To obtain a similar insulating behavior as in the d -only model we increase U and J . Secondly, now also the DC correction has a non-trivial effect, since it shifts the correlated t_{2g} states relative to the oxygen bands. The t_{2g} weight on the oxygen bands is rather

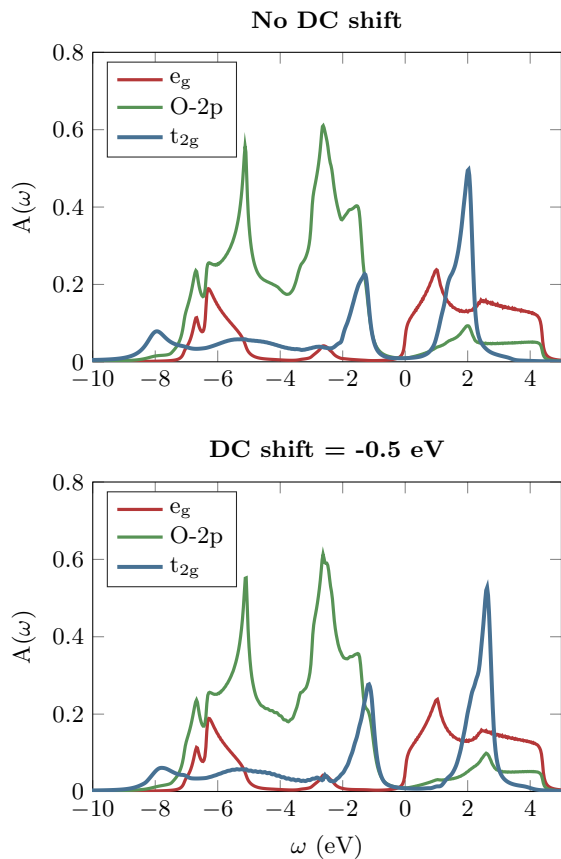


FIG. 5. 3-band d - dp model: effect of the DC correction. *Top*: FLL DC, *Bottom*: FLL DC with an additional shift of -0.5 eV. $U = 5.0$ eV and $J = 0.7$ eV are used as interaction parameters. Contrary to all other figures, in this plot we show the spectrum of the correlated local Green's function.

small, which means that the effect of the DC correction on the HESW is equally low. Thirdly, in the 3-band d - dp model the impurity occupation grows (the exact value depending on U and J), changing the character of the ground state to a mix of states with mainly three and four particles on the impurity, while in the 3-band d -only calculation the occupation of the impurity was three electrons. Due to the increased complexity of the ground state, we expect a richer dependence of the spectrum on the interaction parameters U and J .

In Fig. 4 we compare calculations for different values of J (top) and different values of U (bottom). Overall, the spectral functions consist of a (smaller) lower Hubbard band connected to states from the hybridized oxygen bands and an upper steep-like Hubbard band of similar shape as in the d -only calculation. By comparing the two peaks at -6.0 eV and -8.0 eV, we observe that they behave differently when changing U or J . While the former is only affected by J , the latter is not, but shifts with U . The resolution of the structure in the lower-Hubbard-band/HESW complex demonstrates the capabilities of the FTFS solver.

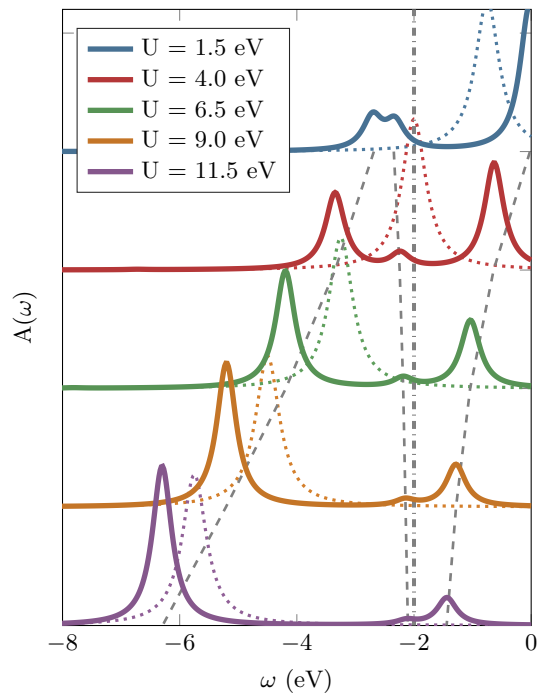


FIG. 6. Spectrum of a one-band AIM with one interacting site coupled to a single non-interacting site (Eq. 3). The spectrum is calculated with the absolute ground state over all particle number sectors. The on-site energy ϵ_1 is shown as gray dashed-dotted vertical line. The gray dashed lines visualize the evolution of the location of the three peaks as a function of the interaction strength U . The colored dotted peaks show the atomic spectrum with peaks at $-U/2$. The upper Hubbard band (additional peak at $\omega > 0$) is not shown. All spectra have been broadened by $\eta_{FT} = 0.2$ eV.

The t_{2g} gap grows when increasing either U or J , which is a typical sign of Mott physics at half filling³⁹. Nevertheless, in the d - dp model the gap size increases slowly: when increasing U by 1.0 eV, the gap only grows by about half of that. Considering also the uncorrelated e_g orbitals, we observe that the single-particle gap is not much affected by the interaction values studied. An artificial lowering of the DC correction by -0.5 eV, which corresponds to a relative shift in energy between the correlated subspace and the uncorrelated states, also increases the t_{2g} gap (Fig. 5). This growth of the gap is mostly due to a shift of the t_{2g} upper Hubbard band, since the chemical potential is pinned by the e_g bands. The first excitation below E_F has a mix of t_{2g} and O- p character. This indicates that in this model, SrMnO₃ is not a pure Mott insulator, but a mixture between Mott- and charge transfer insulator. This classification is consistent with previous results^{8,9,11,13}.

Let us employ a simple toy model to qualitatively understand this intermediate regime. We use a correlated

site coupled to only one non-interacting site:

$$H = U(n_{0,\uparrow} - 0.5)(n_{0,\downarrow} - 0.5) + \sum_{\sigma} V_1(c_{0,\sigma}^{\dagger}c_{1,\sigma} + h.c.) + \epsilon_1 n_{1,\sigma} \quad (3)$$

The purpose of the non-interacting site is to mimic the effect of the HESW. We set the on-site energy to $\epsilon_1 = -2.0$ eV and use a coupling to the impurity of $V_1 = 1.0$ eV. Since we want to understand the occupied part of the spectrum, we focus on negative energies only. In Fig. 6 we show the resulting spectral functions ($\omega < 0$) for various values of the interaction strength U (full lines). The atomic excitation spectra of this model (corresponding to $V_1 = 0$), whose peaks are positioned exactly at $-U/2$, are indicated by dotted lines. This toy model shows three important features:

First: The peak highest in energy (above -2.0 eV) corresponds to the lower Hubbard band for small values of U ⁴¹. We see that it does not cross the on-site energy ϵ_1 with increasing U , but approaches it asymptotically. The bath site *repels* this level and upon increasing U its weight decreases.

Second: The peak lowest in energy shows the opposite behavior. The uncorrelated site repels it towards lower energies and the spectral weight increases when we increase U . For large U this level asymptotically approaches the atomic limit at energy $-U/2$ and eventually becomes the lower Hubbard band. These two peaks together form what one could call a split lower Hubbard band.

Third: The excitation at the on-site energy ϵ_1 shifts to lower energy and splits under the influence of U . Upon increasing U , one part develops into the lower Hubbard band discussed above, and the other approaches ϵ_1 from below, with diminishing weight.

The DMFT spectral functions (Fig. 4) also show roughly a 3-peak structure, where the peaks at about -1.5 eV (-8.0 eV) could be the first (last) peak of the split lower Hubbard band of our toy model. The region in between then corresponds to the small, middle peak in the toy model stemming from the HESW.

The repulsion of the first peak explains why increasing U (Fig. 4 lower graph) has only a relatively weak effect on the size of the gap. On the other hand, effectively shifting the oxygen bands with the DC correction to lower energies (Fig. 5) corresponds to shifting the bath energy ϵ_1 . This means that the repulsion gets weaker, which explains the growth of the gap. Furthermore, when increasing U we find that the peak highest in energy gets smaller, while spectral weight is transferred to the lowest energy peak, which is also shifted to lower energies (Fig. 4). Additionally, a lowering of the DC correction leads to an opposite behavior, where the first peak below E_F grows at the expense of the lowest one in energy. Note that the middle region of our DMFT spectrum shows a J -dependence (Fig. 4 top), which cannot be explained by a one-orbital toy model. Using a similar toy model with two orbitals and Kanamori interaction, we indeed observe a splitting proportional to J in the spectra (not

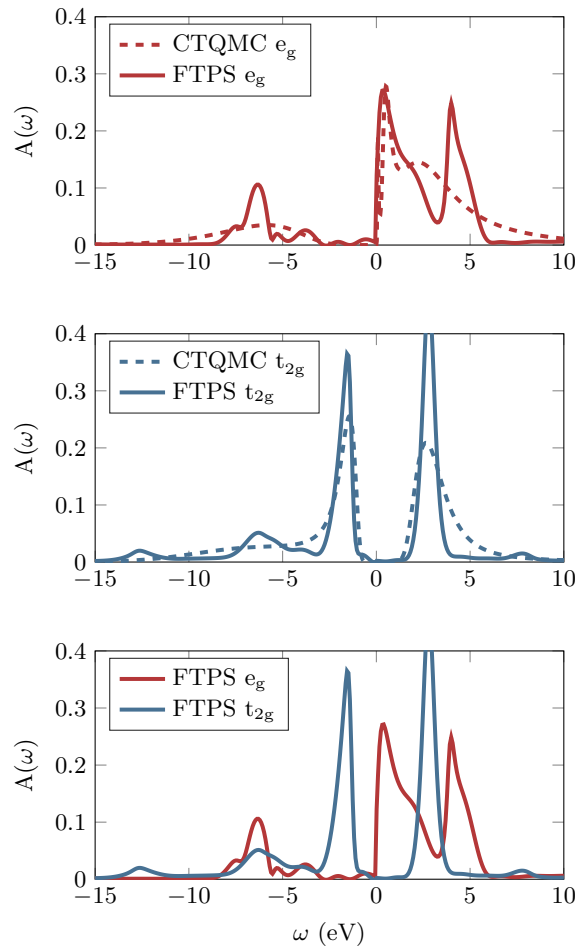


FIG. 7. Comparison of the spectral functions for the 5-band d - dp model between FTPS and CTQMC+MaxEnt. *Top:* e_g orbitals. *Middle:* t_{2g} orbitals. For both calculations we use $U = 6.0$ eV and $J = 0.8$ eV. *Bottom:* Combined spectral function.

shown here). Since the effect is small we will refrain from discussing it in more depth.

We emphasize that the close relation between the toy model and the actual impurity Green's function of SrMnO₃ in the d - dp model suggests that the HESW has the effect of splitting the lower Hubbard band into two bands; their separation increases with the hybridization strength. Therefore, including the oxygen states in the model strongly influences the size of the gap.

C. 5-band d - dp model

From the DFT-DOS in Fig. 1, we see that the e_g orbitals are actually not empty. They possess additional spectral weight at around -7.0 eV, stemming from hybridizations with the oxygen bands. Similarly to the previous section where we included hybridizations of t_{2g} and O- $2p$, we now also include the hybridizations of e_g and

O-2*p*.

As mentioned at the beginning, only approximations to the DC correction are known. For the present 5-band calculation we find that using the FLL DC does not produce a pronounced gap. This can be traced back to the additional hybridizations of e_g with O-2*p* (see discussion below). Furthermore, the FLL formula is based on five degenerate orbitals. In the case at hand we find an approximately half filled t_{2g} impurity ($\langle n_{t_{2g}0\sigma} \rangle \approx 0.5$) and about one electron in total on the e_g part of the impurity ($\langle n_{e_g0\sigma} \rangle \approx 0.2$). One therefore needs to adapt the DC correction to reproduce experimental results. In order to obtain a pronounced gap, we decrease the FLL DC energy by 2.0 eV. Note that it has been argued that very often the FLL-DC is too high²⁵. A reduction of the DC can also be accomplished by adjusting U in the FLL formula^{13,26}.

Fig. 7 shows the spectral function of the full 5-band d - dp calculation with adjusted DC as well as the respective spectral function obtained by a DMFT calculation using CTQMC+MaxEnt. Overall, the FTPS spectrum is in good agreement with the CTQMC+MaxEnt result. However, FTPS provides a much better energy resolution at high energies, which is especially apparent from the pronounced peak structure in the e_g spectrum. From this comparison we also see that the sharp, step-like shape of the e_g spectrum at E_F is not an artifact of the FTPS solver. We note that for the 5-band calculation presented in Fig. 7, FTPS (720 CPU-h) and CTQMC (600 CPU-h) need similar computational effort for one DMFT iteration⁴².

The unoccupied part of the total spectrum (sum of the e_g and t_{2g} spectra shown in the bottom plot of Fig. 7) consists of a three peak structure with alternating e_g - t_{2g} - e_g character, which is much more pronounced than in the 5-band d -only calculation (Fig. 3). Compared to the 3-band d - dp model we find differences mainly in the occupied part of the t_{2g} spectral function (Fig. 9). This is especially apparent in the lowest peak, which seems to be shifted from -9.0 eV to -13.0 eV. Although this high energy excitation is small, the FTPS solver can reliably resolve it.

The differences in the position of this peak are again similar to the behavior of a toy model. Here we use a two-orbital AIM with a single bath site for each orbital:

$$H = H_{\text{int}} + \sum_{m \in (t_{2g}, e_g)} E_m n_{0,m} + \sum_{\sigma} V_m (c_{0,m,\sigma}^{\dagger} c_{1,m,\sigma} + h.c.) + \epsilon_m n_{1,m,\sigma}. \quad (4)$$

For the interaction H_{int} we choose the Kanamori Hamiltonian. As before, we use a single bath site for each orbital to mimic the effect of the HESW. We are interested in the influence of the hybridizations of e_g and O-2*p* on the t_{2g} spectral function. In Fig. 8, we compare the spectrum without e_g -HESW states ($V_{e_g} = 0$) with the one obtained from $V_{e_g} = 2V_{t_{2g}}$ ⁴³. Although one would

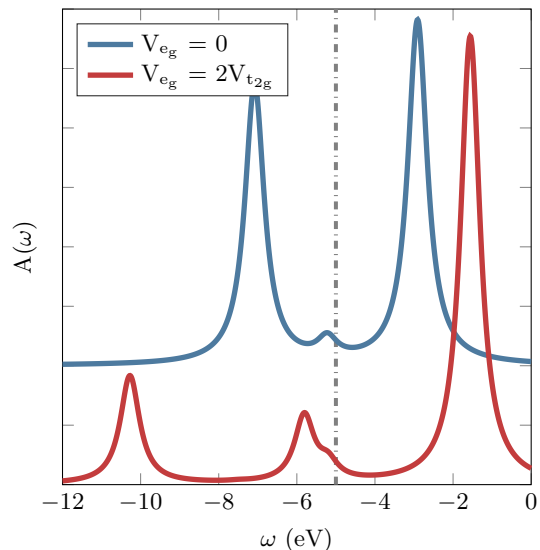


FIG. 8. Effect of the e_g hybridizations on the t_{2g} spectrum of the toy model (Eq. 4). Parameters (in eV): $U = 10.0$, $J = U/10$, $E_{t_{2g}} = -U/2$, $E_{e_g} = -U/2 + 1.0$, $\epsilon_{t_{2g}} = \epsilon_{e_g} = -5.0$ and $V_{t_{2g}} = 1.5$. The grey dashed dotted line shows the bath energy levels. All spectra have been broadened by $\eta_{FT} = 0.2$ eV.

expect the e_g hybridization to only have a minor influence on the t_{2g} spectrum, we observe a rather surprising behavior. The additional hybridization leads to a stronger repulsion of the lowest energy peak from the bath energy, qualitatively explaining the shift from -9.0 eV to -13.0 eV in Fig. 9.

Additionally, this toy model provides an explanation for the necessary adjustment of the DC correction in the 5-band calculation: The peak highest in energy in Fig. 8 is repelled more strongly with the additional e_g hybridizations, therefore the gap decreases. If we would want to obtain a similar t_{2g} gap as with $V_{e_g} = 0$, the interaction in the toy model would need to be increased to $U \approx 20$ eV (keeping $J = U/10$). Since this is unphysical, the only other option is to shift the bath site energies of the toy model. In the DMFT calculation this corresponds to a shift in the DC correction, effectively shifting the HESW to lower energies. This behavior can be observed in Fig. 9, where we compare the spectra of the 3- and 5-band d - dp models. The onset of the lower-Hubbard-band/HESW complex is exactly at the same position in both spectra, although the DC shift differs by 2.0 eV.

IV. COMPARISON TO EXPERIMENT

Equipped with a good understanding of the model-dependent effects on the spectral function, we are finally in a position to compare our results to experiments. Several studies concluded that the unoccupied part of the spectrum consists of three peaks

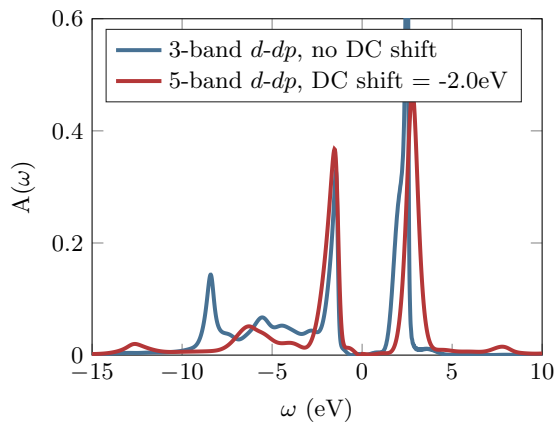


FIG. 9. Comparison of the t_{2g} spectral functions of the 3-band $d-dp$ and 5-band $d-dp$ calculations at $U = 6.0\text{eV}$ and $J = 0.8\text{eV}$, taken from Figs. 4 and 7. In the 5-band calculation we shifted the double counting by -2.0eV to increase the gap. The influence of the number of bands is most apparent in the high-energy features. The increased repulsion of the first peak of the lower-Hubbard-band/oxygen complex (Fig. 8) makes a shift in the DC necessary, if the single particle gap should remain the same.

with alternating e_g - t_{2g} - e_g character¹⁰⁻¹². As we have shown, with DMFT+FTPS we are able to resolve such a structure when including the e_g states as correlated orbitals in a genuine 5-band model. Additionally, we need to choose the energy window, i.e., whether the HESW should be included in the construction of the projective Wannier functions. The nature of the insulating state (Mott or charge transfer) has been debated in the literature^{8,9,11,13}, but it is likely that SrMnO_3 falls in an intermediate regime where a clear distinction is difficult. In the present work we have come to the same conclusion. This implies that the lower Hubbard band and the O-2p bands are not separated in energy, which favors the use of a $d-dp$ model. We therefore conclude that a 5-band $d-dp$ model is necessary to fully capture the low-energy physics of SrMnO_3 .

Having decided on the model for the correlated subspace, we still need to determine the interaction parameters U and J as well as the DC. To do so we use PES and XAS data for the Mn-3d orbitals obtained by Kim *et al.*¹² and compare to our total impurity spectrum ($6A_{t_{2g}}(\omega) + 4A_{e_g}(\omega)$ from Fig. 7). According to Ref. 12, the XAS (PES) spectrum can be considered to represent the unoccupied (occupied) Mn-3d spectrum. In the measured spectrum the chemical potential is in the middle of the gap. In all our calculations, the chemical potential is determined by the onset of the unoccupied e_g spectrum. However, the absolute position in energy is not exactly known in XAS⁴⁴. Our calculation is in good agreement with the experiment when we use a rigid shift of the XAS spectrum by 0.8eV to lower energies. Additionally, we deduce from the peak positions in the experiment that the interaction parameters used

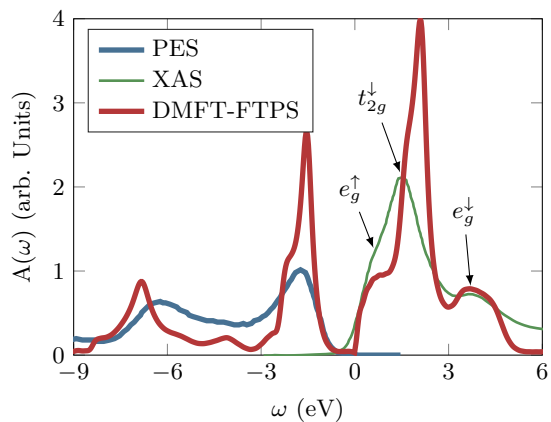


FIG. 10. Photo Emission Spectroscopy (PES) and X-ray Absorption Spectroscopy (XAS) compared to the 5-band $d-dp$ DMFT-FTPS results ($U = 5.0\text{eV}$ and $J = 0.6\text{eV}$). The experimental curves are reproduced from Ref. 12, Fig. 5. We normalized the experimental curves to $\int_{-9}^0 A_{\text{PES}} d\omega = \int_{-9}^0 A_{\text{FTPS}} d\omega$ and $\int_0^6 A_{\text{XAS}} d\omega = \int_0^6 A_{\text{FTPS}} d\omega$. FTPS as well as the experiments show a 3-peak structure of alternating e_g - t_{2g} - e_g character in the unoccupied part of the spectrum (indicated by arrows). For the arrow labels we adopted the notation of Ref. 12, where e_g^\uparrow means an excitation into the e_g spectrum with majority spin, while t_{2g}^\downarrow and e_g^\downarrow are excitations into the t_{2g} and e_g spectrum with minority spin (see also Eq. 2).

for the calculations presented in Fig. 7 are too high. The separation of the two e_g peaks ($\sim J$) and also the relative position of the t_{2g} upper Hubbard band is different than in the experiment. Therefore, we decrease the interaction parameters to $U = 5.0\text{eV}$ and $J = 0.6\text{eV}$ but keep the static shift of the FLL DC by -2.0eV . Note that these parameters are similar to the ones used in other DFT+DMFT studies on SrMnO_3 ^{13,14}.

The resulting spectral function for the new set of parameters is compared to the experimental spectrum in Fig. 10. Notably, the bandwidths of both, the unoccupied and the occupied spectrum, agree very well with the experiment. The unoccupied part of the experimental spectrum (XAS) shows that the first e_g peak is just a shoulder of the t_{2g} upper Hubbard band, and that the separation of the two e_g peaks is about 3.2eV , which is in agreement with our result. Since this separation is proportional to the Hund's coupling, we conclude that $J \approx 0.6\text{eV}$ for this compound. The t_{2g} upper Hubbard band at 2.0eV is still slightly too high in energy.

The experiment also shows a lower-Hubbard-band/oxygen complex with two main peaks at about -6.0eV and -2.0eV . As discussed in the previous sections (bottom plot of Fig. 7), our results identify the first peak at -2.0eV to have mainly t_{2g} character and to correspond to the largest part of the split lower Hubbard band, whereas the second peak at -6.0eV has both e_g and t_{2g} character and stems from the hybridizations with

the oxygen bands. We note that the region between these two peaks has larger spectral weight in the experiment than in our calculations. Importantly, no prominent spectral features are observed in the experiment around -8.0 eV, strengthening our conclusion that the 3-band d - dp model is not sufficient to describe the experiment (see also Fig. 9).

V. CONCLUSIONS

We have studied the influence of the choice of the correlated subspace, i.e. the number of bands and the energy window, on the DFT+DMFT result for the strongly correlated compound SrMnO₃. For d -only models (neglecting p - d hybridizations), we have shown that the empty e_g orbitals should be included in the correlated subspace because interactions with the half-filled t_{2g} bands affect the spectrum, leading to a multiplet structure and a broadening of the e_g DFT-DOS. Including the Mn- $3d$ /O- $2p$ hybridizations in a 3-band model for the t_{2g} bands only, i.e., the 3-band d - dp model, we found a situation similar to avoided crossing, which leads to an interesting interplay of atomic physics (lower Hubbard band) and Mn- d /O- p hybridizations. In SrMnO₃, the lower Hubbard band hybridizes with the t_{2g} Wannier-weight on the oxygen bands, giving rise to a spectrum that can be approximated by three peaks. This result provides new perspectives on an intermediate regime, where both Mott and charge transfer physics are found. By performing a 5-band calculation including the p - d hybridization, we

investigated the effect of the e_g hybridization on the t_{2g} spectrum. The splitting due to avoided crossing is heavily increased, which strongly affects the 3-peak structure and also decreases the gap. Equipped with a good understanding of the different correlated subspaces and the effects of the model parameters (U , J , DC) we were able to obtain a spectral function in good agreement with experimental data. We conclude that the choice of a suitable model for the correlated subspace is important, since the inclusion of both the O- $2p$ hybridizations and the e_g states is essential for a correct description of the observed spectral function in SrMnO₃.

Finally, we would also like to stress that we have shown that FPTS is a viable real-time impurity solver for real material calculations with five bands.

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